## CHEM 116 - Honors and Majors General and Analytical Chemistry I

3 Exams, 9 Quizzes, 10 Labs, 12 Weeks HWK - 865 points (1245 in course)

EIII: AVE $=95$ (63\%) Range: 36-146
EII: AVE = 106 (71\%)
El: $\quad$ AVE $=87$ (58\%)

| Q1 | 6.0 | Q5 | 6.6 | Q8 | 6.4 |
| :--- | :--- | :--- | :--- | ---: | :--- |
| Q3 | 4.2 | Q6 | 6.2 | Q9 | 8.3 |
| Q4 | 7.8 | Q7 | 6.1 | Q10 | 4.9 |


| E1 | 19.4 |
| :--- | :--- |
| E2 | 17.3 |
| L3 | 18.4 |

Q10 4.9

4-4 15.9
E8 14.8
10.5
class average 71.2\%

Class Averages

| EXAM | 288 | $64 \%$ |
| :--- | :---: | :---: |
| QZ | 57 | $63 \%$ |
| LAB | 150 | $75 \%$ |
| HWK | 102 | $82 \%$ |

Course Grade Estimate
A 75\%
B $65 \%$
C $50 \%$
D $40 \%$

## Polyprotic Acids and Bases - Intermediate Form

Consider a diprotic acid

$$
\mathrm{H}_{2} \mathrm{~A}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \Leftrightarrow \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{HA}^{-}(a q) \text { base }
$$

$$
\text { acid } \mathrm{HA}^{-}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \Leftrightarrow \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{A}^{2-}(a q)
$$

If $\mathrm{H}_{2} \mathrm{~A}$ is a weak acid its conjugate base, $\mathrm{HA}^{-}$is amphoteric. It can act as an acid (second equation) or as a base (reverse of first reaction). What is the pH of a solution of $\mathrm{HA}^{-}$such as NaHA?
Exact Treatment (H pp. 216-218) for NaHA
species: $\mathrm{H}_{2} \mathrm{~A}, \mathrm{HA}^{-}, \mathrm{A}^{2-}, \mathrm{H}^{+}, \mathrm{OH}^{-}, \mathrm{Na}^{+}=>$need 6 equations
charge balance: $\left[\mathrm{H}^{+}\right]+\left[\mathrm{Na}^{+}\right]=\left[\mathrm{HA}^{-}\right]+2\left[\mathrm{~A}^{2-}\right]+\left[\mathrm{OH}^{-}\right]$
material balance: $\mathrm{M}_{\mathrm{NaHA}}=\left[\mathrm{Na}^{+}\right]=\left[\mathrm{H}_{2} \mathrm{~A}\right]+\left[\mathrm{HA}^{-}\right]+\left[\mathrm{A}^{2-}\right]$
equilibria: $\quad K_{\mathrm{a} 1}=\frac{\left[\mathrm{H}^{+}\right]\left[\mathrm{HA}^{-}\right]}{\left[\mathrm{H}_{2} \mathrm{~A}\right]} \quad K_{\mathrm{a} 2}=\frac{\left[\mathrm{H}^{+}\right]\left[\mathrm{A}^{2-}\right]}{\left[\mathrm{HA}^{-}\right]} \quad K_{\mathrm{w}}=\left[\mathrm{H}^{+}\right]\left[\mathrm{OH}^{-}\right]$
One can show that

$$
\left[\mathrm{H}^{+}\right]^{2}=\frac{K_{\mathrm{a} 1} K_{\mathrm{a} 2}\left[\mathrm{HA}^{-}\right]+K_{\mathrm{a} 1} K_{\mathrm{w}}}{K_{\mathrm{a} 1}+\left[\mathrm{HA}^{-}\right]}
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## Polyprotic Acids and Bases - Intermediate Form

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1. when the major species is $\mathrm{HA}^{-}=>\left[\mathrm{HA}^{-}\right]=\mathrm{M}_{\text {HA- }}\left(\mathrm{F}_{\text {HA- }}\right)$

$$
\approx \frac{K_{\mathrm{a} 1} K_{\mathrm{a} 2} \mathrm{M}_{\mathrm{NaHA}}+K_{\mathrm{a} 1} K_{\mathrm{w}}}{K_{\mathrm{a} 1}+\mathrm{M}_{\mathrm{NaHA}}}-\frac{K_{\mathrm{a} 1}\left(K_{\mathrm{a} 2} \mathrm{M}_{\mathrm{NaHA}}+K_{\mathrm{w}}\right)}{K_{\mathrm{a} 1}+\mathrm{M}_{\mathrm{NaHA}}}
$$

2. often $K_{\mathrm{w}} \ll K_{\mathrm{a} 2} \mathrm{M}_{\mathrm{NaHA}}$

$$
\approx \frac{K_{\mathrm{a} 1} K_{\mathrm{a} 2} \mathrm{M}_{\mathrm{NaHA}}}{K_{\mathrm{a} 1}+\mathrm{M}_{\mathrm{NaHA}}}
$$

3. and $K_{\mathrm{al} 1} \ll \mathrm{M}_{\mathrm{NaHA}}$ this often needs to be checked

$$
\approx \frac{K_{\mathrm{a} 1} K_{\mathrm{a} 2} \mathrm{M}_{\mathrm{NaHA}}}{\mathrm{M}_{\mathrm{NaHA}}}=K_{\mathrm{a} 1} K_{\mathrm{a} 2}
$$

or

$$
\mathrm{pH}=\frac{1}{2}\left(\mathrm{p} K_{\mathrm{a} 1}+\mathrm{p} K_{\mathrm{n} 2}\right)
$$

## Polyprotic Acids and Bases - Predominant Species

$$
\mathrm{pH}=\mathrm{p} K_{\mathrm{a}}+\log _{10} \frac{[\mathrm{~B}]}{[\mathrm{A}]}
$$



## Fractional Composition Diagrams, $\alpha$ versus pH


monoprotic acid, HA

diprotic acid, $\mathrm{H}_{2} \mathrm{~A}$

## FIND EQUIVALENCE POINT FIRST

## CORRECT MOLARITY AS TITRANT IS ADDED

## 11-1 Strong Acid/Base

11-2 Weak Acid with Strong Base
11-3 Weak Base with Strong Acid
11-4 Polyprotic Titrations
no quiz next week
homework for week 14,15
due dates next Wednesday and Friday
lab notebooks due next Wednesday in discussion

## Acid-Base Titrations

"Learn to recognize buffers! They lurk in every corner of acid-base chemistry."

## Acid-Base Titrations

Solution of a base of known concentration is added to an acid of unknown concentration (or acid of known concentration added to a base of unknown concentration)
titrant
titration curve
equivalence point half-equivalence point
$\mathrm{pH}>7$ titrating weak acid
$\mathrm{pH}=7$ titrating strong acid or base
$\mathrm{pH}<7$ titrating weak base
endpoint

## Acid-Base Titrations - Strong

strong acid or strong base titration overview
classic Arrhenius neutralization reaction characterized by strong acid (base):
strong base (acid) titrant:
total ionic equation:
net ionic equation (what is $K$ ?):
titration curve - one inflection point (equivalence point)


## Strong Base Titrations

EX 1. Determine the pH for titration of 50.00 mL of 0.02000 M KOH with 0.1000 M HBr .

| Excess <br> $\mathbf{O H}^{-}$ | Excess <br> $\mathbf{H}^{+}$ |
| :---: | :---: |



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$\mathrm{pH}=\mathrm{pK}_{\mathrm{w}}-\mathrm{pOH}, \quad \mathrm{pK}_{\mathrm{w}}=$ $-\log \left(1.01 \times 10^{-14}\right)=13.9956$

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\mathrm{pH}=13.9956+\log (0.02000)=12.2966=>12.297
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\mathrm{pH}=13.9956+\log \{[50(0.02)-3(0.1)] / 53\}=12.116
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K_{\mathrm{w}}=\left[\mathrm{H}^{+}\right]^{2}=>\left[\mathrm{H}^{+}\right]=\sqrt{ } K_{\mathrm{w}}=>\mathrm{pH}=1 / 2 \mathrm{p} K_{\mathrm{w}}=13.9956 / 2=6.998
$$

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d) when 10.50 mL of HBr is added excess $\mathrm{H}^{+}$
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$$

d) when 10.50 mL of HBr is added excess $\mathrm{H}^{+}$

$$
\mathrm{pH}=-\log \{[(10.5)(0.1)-50(0.02)] / 60.5\}=3.0827=>3.083
$$

$\mathrm{pH}=\mathrm{pK}_{\mathrm{w}}-\mathrm{pOH}, \quad \mathrm{p} K_{\mathrm{w}}=$ $-\log \left(1.01 \times 10^{-14}\right)=13.9956$

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| :---: | :---: |



## Weak Acid Titrations

EX 2. 50.00 mL 0.02000 M MES [2-(N-morpholino)ethanesulfonic acid, pKa = 6.27] titrated with 0.1000 M NaOH .


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b) when 3.00 mL of NaOH is added buffer, $\left.\mathrm{pH}=p K_{\mathrm{a}}+\log [\mathrm{A}]\right][\mathrm{HA}]$


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d) when 10.10 mL of NaOH is added excess $\mathrm{OH}^{-}$


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$$

d) when 10.10 mL of NaOH is added excess $\mathrm{OH}^{-}$

$$
\mathrm{pH}=13.9956+\log \{[(10.1)(0.1)-50(0.02)] / 60.1\}=10.22
$$



## Acid-Base Titrations - Weak

weak acid (base) titrated with strong base (acid):
weak acid (base):
strong base (acid) titrant:
total ionic equation:


## Polyprotic Titrations (Mostly Treated as a Buffer)

$$
\mathrm{H}_{3} \mathrm{~A} \quad \rightarrow \quad \mathrm{H}_{2} \mathrm{~A}^{-} \quad \rightarrow \quad \mathrm{HA}^{2-} \quad \rightarrow \quad \mathrm{A}^{3-}
$$



## Levelling Effect

| Acidity Constants in Water at $25^{\circ} \mathrm{C}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Acid | Formula | Conjugate Base | K | pK ${ }_{\text {a }}$ |
| Hydriodic | HI | $\mathrm{I}^{-}$ | $\Rightarrow 10^{11}$ | \% -11 |
| Hydrobromic | HBr | $\mathrm{Br}^{-}$ | $\Rightarrow 10^{9}$ | $\Rightarrow-9$ |
| Perchloric | $\mathrm{HClO}_{4}$ | $\mathrm{ClO}_{4}^{-}$ | $=10^{7}$ | $\approx-7$ |
| Hydrochloric | HCl | $\mathrm{Cl}^{-}$ | $=10^{7}$ | $=-7$ |
| Chloric | $\mathrm{HClO}_{3}$ | $\mathrm{ClO}_{3}^{-}$ | $=10^{3}$ | $=-3$ |
| Sulfuric (1) | $\mathrm{H}_{2} \mathrm{SO}_{4}$ | $\mathrm{HSO}_{4}^{-}$ | $=10^{2}$ | $=-2$ |
| Nitric | $\mathrm{HNO}_{3}$ | $\mathrm{NO}_{3}^{-}$ | $\Rightarrow 20$ | $=-1.3$ |
| Hydronium ion | $\mathrm{H}_{3} \mathrm{O}^{+}$ | $\mathrm{H}_{2} \mathrm{O}$ | 1 | 0.0 |
| Urea acidium ion | $\left(\mathrm{NH}_{2}\right) \mathrm{CONH}_{3}^{+}$ | $\left(\mathrm{NH}_{2}\right)_{2} \mathrm{CO}$ (urea) | $6.6 \times 10^{-1}$ | 0.18 |
| Iodic | $\mathrm{HIO}_{3}$ | $1 \mathrm{O}_{3}^{-}$ | $1.6 \times 10^{-1}$ | 0.80 |
| Oxalic (1) | $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}$ | $\mathrm{HC}_{2} \mathrm{O}_{4}^{-}$ | $5.9 \times 10^{-2}$ | 1.23 |
| Sulfurous (1) | $\mathrm{H}_{2} \mathrm{SO}_{3}$ | $\mathrm{HSO}_{3}^{-}$ | $1.5 \times 10^{-2}$ | 1.82 |
| Sulfuric (2) | $\mathrm{HSO}_{4}^{-}$ | $\mathrm{SO}_{4}^{2-}$ | $1.2 \times 10^{-2}$ | 1.92 |
| Chlorous | $\mathrm{HClO}_{2}$ | $\mathrm{ClO}_{2}^{-}$ | $1.1 \times 10^{-2}$ | 1.96 |


| Sulfurous (2) | $\mathrm{HSO}_{3}^{-}$ | $\mathrm{SO}_{3}^{2-}$ | $1.0 \times 10^{-7}$ | 7.00 |
| :--- | :--- | :--- | :--- | :--- |
| Arsenic (2) | $\mathrm{H}_{2} \mathrm{AsO}_{4}^{-}$ | $\mathrm{HAsO}_{4}^{2-}$ | $9.3 \times 10^{-8}$ | 7.03 |
| Hydrosulfuric | $\mathrm{H}_{2} \mathrm{~S}$ | $\mathrm{HS}^{-}$ | $9.1 \times 10^{-8}$ | 7.04 |
| Phosphoric (2) | $\mathrm{H}_{2} \mathrm{PO}_{4}^{-}$ | $\mathrm{HPO}_{4}^{2-}$ | $6.2 \times 10^{-8}$ | 7.21 |
| Hypochlorous | HClO | $\mathrm{ClO}^{-}$ | $3.0 \times 10^{-8}$ | 7.52 |
| Hydrocyanic | HCN | $\mathrm{CN}^{-}$ | $6.2 \times 10^{-10}$ | 9.21 |
| Ammonium ion | $\mathrm{NH}_{4}^{-}$ | $\mathrm{NH}_{3}$ | $5.6 \times 10^{-10}$ | 9.25 |
| Carbonic (2) | $\mathrm{HCO}_{3}^{-}$ | $\mathrm{CO}_{3}^{2-}$ | $4.8 \times 10^{-11}$ | 10.32 |
| Methylammonium ion | $\mathrm{CH}_{3} \mathrm{NH}_{3}^{+}$ | $\mathrm{CH}_{3} \mathrm{NH}_{2}$ | $2.3 \times 10^{-11}$ | 10.64 |
| Arsenic (3) | $\mathrm{HAsO}_{4}^{2-}$ | $\mathrm{AsO}_{4}^{3-}$ | $3.0 \times 10^{-12}$ | 11.52 |
| Hydrogen peroxide | $\mathrm{H}_{2} \mathrm{O}_{2}$ | $\mathrm{HO}_{2}^{-}$ | $2.4 \times 10^{-12}$ | 11.62 |
| Phosphoric (3) | $\mathrm{HPO}_{4}^{2-}$ | $\mathrm{PO}_{4}^{1-}$ | $2.2 \times 10^{-13}$ | 12.66 |
| Water | $\mathrm{H}_{2} \mathrm{O}^{-}$ | $\mathrm{OH}^{-}$ | $1.0 \times 10^{-14}$ | 14.00 |
| Hydrogen sulfide ion | $\mathrm{HS}^{-}$ | $\mathrm{S}^{2-}$ | $1.0 \times 10^{-19}$ | 19.00 |
| Hydrogen | $\mathrm{H}_{2}$ | $\mathrm{H}^{-}$ | $1.0 \times 10^{-33}$ | 33.00 |
| Ammonia | $\mathrm{NH}_{3}$ | $\mathrm{NH}_{2}^{-}$ | $1.0 \times 10^{-38}$ | 38.00 |
| Hydroxide ion | $\mathrm{OH}^{-}$ | $\mathrm{O}^{2-}$ |  |  |

acids stronger
than $\mathrm{H}_{3} \mathrm{O}^{+}$
conjugate bases
stronger than $\mathrm{OH}^{-}$

